FACULTY OF PHYSICS, UNIVERSITY OF RIJEKA 19. 4. 2024.

# WORKSHOP LIGHT AND PHOTOSYNTHESIS IN THE SEA

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# Fragility of primary production under climate change

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# Motivation



Adopted from Limits to growth (1972)

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Where are we now?



Anthropogenic carbon emissions per year 10 Gt C Carbon assimilated by the biosphere per year 100 Gt C Carbon assimilated by phytoplankton 50% of total Phytoplankton biomass 1% of total land biomass

## How we got here

Global annual marine primary production from the literature



- Steeman Nielsen & Jensen, 1957
- Gessner, 1957
- Koblenz-Mishke, 1970
- Platt & Subba Rao, 1975
- Eppley & Peterson, 1979
- Berger et al., 1987
- Longhurst et al., 1995
- Antoine et al., 1996
- Behrenfeld & Falkowski, 1997
- Melin, 2003
- Behrenfeld et al., 2005
- Westberry et al., 2008
- Buitenhuis et al., 2013
- Kulk et al., 2021

Adopted from Buitenhuis et al. (2013)

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# Where are we going?

#### Tragedy of the commons

If decisions about the use of renewable natural resources are based exclusively on profits, even long-term profits, renewable natural resources will be used on a sustainable basis only if their biological growth rate is greater than the expected growth rate of alternative investments. Because the growth rate of the world economy today is greater than the biological growth rate of most renewable resources, there are powerful economic incentives not to use renewable natural resources on a sustainable basis. If people accept the rules of the game in a free market economy, it is rational to use renewable resources unsustainably whenever biological production fails to compete with alternative forms of investment.

(Marnet, 2001)

# The beginning for me



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At the end of 2010 I was given teaching materials written by Trevor Platt & Shubha Sathyendranath from the Plymouth Marine Laboratory in the United Kingdom.

Here is an excerpt from those materials:

In this series of articles, we propose to develop, in a systematic and self-consistent manner, the theoretical basis for calculating primary production in aquatic systems. The material should be accessible and understandable by anyone with a working knowledge of **elementary calculus**.

Just got my masters in Physics, so elementary calculus was not that hard ;)

# What happens below the surface?



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# Trevor's mathematical formalism and the canonical model

$$P_{Z,T} = \int_{0}^{\infty} \int_{0}^{D} Bp^{B}(I) \,\mathrm{d}t \,\mathrm{d}z$$

So far so good!

# Trevor's exact solution (Platt et al., 1990)

$$P_{Z,T} = \frac{BP_m^B D}{K} \left( \sum_{n=1}^{\infty} \frac{2\left(I_*^m\right)^{2n-1}}{\pi \left(2n-1\right) \left(2n-1\right)!} \frac{\left(2n-2\right)!!}{\left(2n-1\right)!!} - \sum_{n=1}^{\infty} \frac{\left(I_*^m\right)^{2n}}{2n \left(2n\right)!} \frac{\left(2n-1\right)!!}{\left(2n\right)!!} \right)^{2n} \frac{\left(2n-1\right)!!}{\left(2n\right)!!} \right)^{2n} \frac{\left(2n-1\right)!!}{\left(2n-1\right)!!} + \frac{\left(2n-1\right)!!}{\left(2n-1\right)!!} - \frac{\left(2n-1\right)!!}{\left(2n-1\right)!!} \frac{\left(2n-1\right)!!}{\left(2n-1\right)!!} + \frac{\left(2n-1\right)!}{\left(2n-1\right)!!} + \frac{\left(2n-1\right)!}{\left(2n-1\right)!!} + \frac{\left(2n-1\right)!}{\left(2n-1\right)!} + \frac{\left(2n-$$

Talk about elementary calculus! What are theses double exclamations?!

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# Vertical structure

# **Primary production**

 $P(z,t) \quad [mg C m^{-3} h^{-1}]$ 

# $\begin{array}{ll} \textbf{Daily production} \\ P_T\left(z\right) & \left[ \operatorname{mg} \operatorname{C} \operatorname{m}^{-3} \right] \end{array}$

# Watercolumn production

 $P_{Z,T} \,[\,{
m mg}\,{
m C}\,{
m m}^{-2}\,]$ 



# Approaches to studying primary production

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#### In situ

Incubation at sea under natural light conditions. (Steemann Nielsen, 1952)

# In vitro

Incubation under controlled light conditions. (Platt i Jassby, 1976)

# In silico

Computer implementation of primary production models. (Gentleman, 2002)

#### Steemann Nielsen (1952) ICES Journal of Marine Science

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The Use of Radio-active Carbon (C<sup>14</sup>) for Measuring Organic Production in the Sea.

> E. Steemann Nielsen, Royal Danish School of Pharmacy, Copenhagen

#### 1. Introduction.

As on land, uo in the sca autotrophic plants are the basis of all life. Scalie plants, however, live on a narrow ringea long the coasts only. If we wish to consider the amount of matter produced annually by the plants of the say, which are found everywhere in the upper water-masses of the sas. It is the organic matter synthesized by the plants on algae out indirectly servers as food for all organisms in the sea, from the smallert bacteria to the largest which.

As the constantly increasing number of human beings on our globe requires greater and greater quantities of food, and as the food production on land can be but little increased, we must consider the sea as an important reserve.

It is therefore of great importance to be able to estimate the amount of the annual production by the plants of the east. In recent years one has repeatedly come across figures according to which the annual production of ngamic matter in the east in nearly tree times that of the productions on land. These figures originate from R ab in  $\alpha$  witch the structure of the structure of the structure of the structure of the production of the structure of the structu

Whereas, according to R a bin ow it c h, the land annually fixes  $1-9\times10^{10}$  tons of carbon, a value originally calculated by S c h r o e d e r (1919), the sca is said to fix  $15+5\times10^{10}$  tons of carbon.

Both Riley's and Seiwell's figures for the production of organic matter in the tropical Atlantic seem incredible, even before determinations were made by the "Galathea" Expedition, and, indeed. E. Steemann Nielsen

in what follows it will be shown that even the order of magnitude is wrong.

Brow the "Galarka" Explicition put to see in October 1950, the production of organism matter in the occas must therefore the considered as completely unknown. Oth values for the production in a few methods which is vocid normally be impossible to as one the open ratt is therefore highly significant that the expetition was provided with explanent for determining the production of matter by phytophakaton active carbon incorps CV in mo its service, has now been used by the "Galarka" Experiment and the ordicative of the area was very high equal certainty whether the productivity of the usa area was very high the production of matter in the scores, a war rate on broad lines.

#### 2. Methods previously used for Determining the Production of Matter in the Sea.

The first arcempts at determining the production of organic matter in a costart argoin were made in the English Channel (A K is n. § 1922, 1923). Until them scientrists had had to content themselves with investigations of the magnitude of the standing crop of plants, Observations of this kind are of course of great interest in themselves. In many production of matter, we approximate the determination of the production of matter.

To take an example from the land, if immediately before the harvest we compare the quanties of matter found per again enter of sufficient a constituted and a word, by far the gravest amount of organic accoundanced during a long series of yours, whereas all the organic matter in the confided has here preduced in a single season. If the production of matter in the two locations is no the determined in matter as the sense of the season of the season of the production of matter in the two locations is no the determined in matter produced in a year through phonosymbolis, thus getting the grass production. If we deduct from this quantity the reprivation of the phase, during the year, we shall get the net production, Boh the during the years are as the for experiment of the phase.

The quantity of matter in the plankton in a tea area at a certain time cannot, of course, be compared further truty with the amount of matter in the land regions mentioned above, as the matter in the sach has been produced in a very short proved, often only a few days. If the production of matter by the plankton always took place at the same tates is would of course be possible to compare the productivity of the plankton in the various areas on the basis of the amount of planktone present, unriting what matter of devices importance for the trat of or ordenicions.

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As the constantly increasing number of human beings on our globe requires greater and greater quantities of food, and as the food production on land can be but little increased, we must consider the sea as an important reserve.

# Some in situ time series of primary production that I had access to at that time

Stončica	1962	
Kaštelanski zaljev	1962	
Bermuda Atlantic Time Series	1988	bats.bios.edu
Hawaii Ocean Time Series	1988	hahana.so est.hawaii.edu/hot/hot-dogs
Monterey Bay	1988	www.mbari.org/bog
La Coruña	1990	www.seriestemporales-ieo.com
Western Channel Observatory	1992	www.western channel observatory.org.uk
Cariaco	1996	imars.marine.usf.edu/car

- + 1148 annual time series from 483 locations (Cloern et al., 2014)
- + 125 time series longer than 8 years with more than 10 measurements per year (Winder & Cloern, 2010)

# Mathematical formalism

#### **Primary production**

$$P(z,t) = B(z) p^B \left( I(z,t) \right)$$

#### Daily production

$$P_{T}(z) = \int_{0}^{D} B(z) p^{B} \left( I(z,t) \right) dt$$

#### Watercolumn production

$$P_{Z,T} = \int_{0}^{\infty} \int_{0}^{D} B(z) p^{B} \left( I(z,t) \right) dt dz$$



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# Underwater light field





 $I(0) = I_0$ 

Beer-Lambert law

 $\frac{\partial I}{\partial z} = -KI$ 

Irradiance at depth

 $I(z) = I_0 \exp\left(-Kz\right)$ 

## Example



# Photosynthesis irradiance function



$$p^{B}(I) = P_{m}^{B} \left( 1 - \exp\left(-\alpha^{B} I / P_{m}^{B}\right) \right)$$

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# Parameters at Hawaii

# Parameters at Bermuda



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# Example



# Biomass profile



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# Canonical solution for daily production at depth



 $P_T(z) = B(z)P_m^B Df_z(I_m^*)$ 

(Kovač et al., 2016)

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# Daily production profile





# Model versus data for production at depth

# Canonical solution for daily watercolumn production



# Model versus data for watercolumn production





Bermuda  $R^2$  0.97



# Where do we use these production models?



Time evolution of phytoplankton biomass B in the ocean is modelled as:

$$\frac{\partial B}{\partial t} = P - L + advection + mixing$$

Change in biomass is a result of production, losses and transport.

# How good are these models?

Time to find out by doing some coding exercises:)